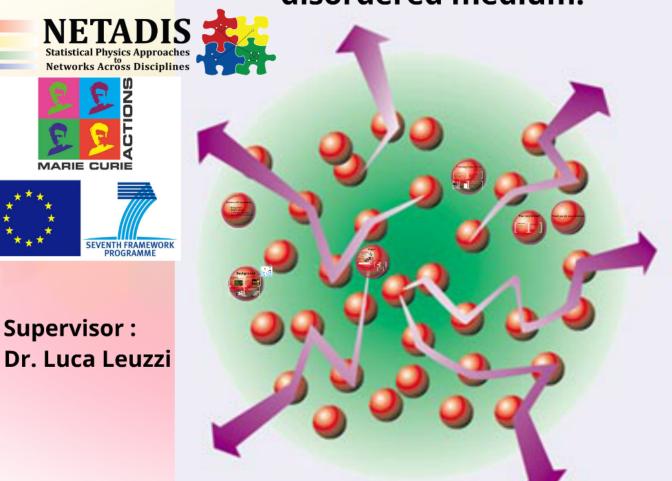
"Inference of coupling of waves in non linear disordered medium."





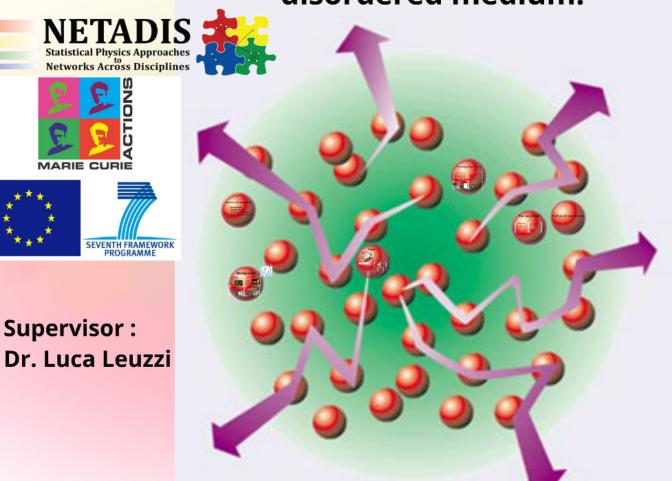


ESR: **Payal Tyagi** 



**Supervisor:** 

"Inference of coupling of waves in non linear disordered medium."







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## **Scheme of Presentation**

- Background
- Project details
- Training experience
- Applications and future



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## **BS** Physics

St. Stephen's College, University of Delhi, New Delhi, India

2007-10



## Early Stage Reseacher/ PhD student

IPCF-CNR/ Sapienza University, Rome

starting: Nov 2012



ARABIAN SEA

## **MSc Physics**

Banasthali University, Rajasthan, India

2010-12

Focus : Condensed Matter Physics



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" Crystal- chemical comparative study between naturally occuring shpene crystals."

Bhabha Atomic Research Centre(BARC), Mumbai, India

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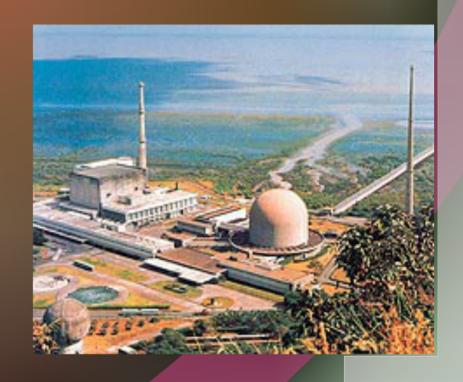


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# **Project**

## System under consideration

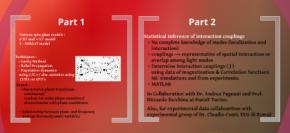
- Statistical mechanics of disordered system
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- Spins(conitnous) -> mode phases, mode amplitude
- Graph (various) -> modes network
- Non linear interaction -> laser medium



Generic Hamiltonian:

$$\mathcal{H} = -\Reigg[\sum_{j < k} G_{jk}^{(2)} a_j a_k^* + \sum_{\omega_j + \omega_k = \omega_l + \omega_m} G_{jklm}^{(4)} a_j a_k a_l^* a_m^*igg]$$

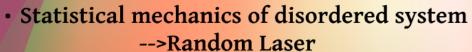
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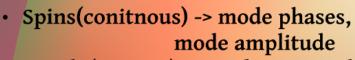


various generic graphs from short to long

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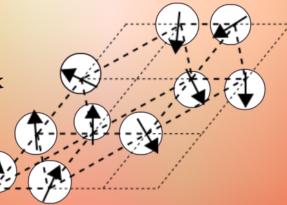
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- Relationship between phase and frequency
- Various thermodynamic variables

### Part 2

### Statistical inference of interaction couplings

- No complete knowledge of modes (localization and interaction)
- couplings --> representative of spatial interaction or overlap among light modes
- Determine interaction couplings (J)
  using data of magnetisation & Correlation functions
  MC simulations and from experiments.
- MATLAB

In Collaboration with Dr. Andrea Pagnani and Prof. Riccardo Zecchina at HuGeF Torino.

Also, for experimental data collaboartion with experimental group of Dr. Claudio Conti, UOS di Roma)

### Part 3

- · MC simulations on various generic graphs from short to long range
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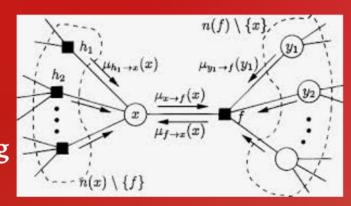
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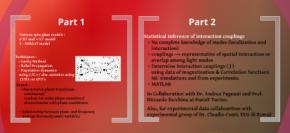
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January 2013 - July 2013

- · Theory and phenomenology of Structural Glass
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#### Investigating random laser through study of disordered systems.

Payal Tyagi and Luca Leuzzi

IPCF-CNR, Dep. of Physics, Sapienza University of Rome, Plazzale A. Moro 2, I-00185, Rome, Italy



Startics from the Hous master equation for mode looking

Hence, the Hamiltonian with 2 body and 4 body terms to-petitor reads:

 $H = -B(\sum_{i \in \mathcal{I}^*} l_{ij}^{(1)} | a_i a_j^* + \sum_{i \in I + a_i = a_i + a_i} l_{ijkl}^{(k)} a_i a_j a_k^* a_i^* |$ where coupling has in built quenched amplitude and modes are required to satisfy the following mode focking condi-tion.

ω<sub>s</sub> being the width of the peak in amplitude spectrum

 $H = -\sum_{i,j} \lambda_i \sigma_i \sigma_j$ 

 $F = -k \sum_{i} F_{i}^{(1)} + \sum_{r \in G_{i}} F_{r \in C_{i}}^{(2)}$ 



The system can be salved by savity method using popular

2009-SAT is a constraint satisfaction patition to solve a system of inner equation which involves finding a vector 2 of backers varieties and subject to 2 of backers varieties scalingly the flower equation ,  $AP = \mathbb{R}_{N} \cdot \text{sol}(1)$ . When mapped into spin glass problem than  $a_1 = (-1)^n$  and  $b_1 = (-1)^n$  and  $a_2 = (-1)^n$  and  $a_3 = (-1)^n$  and the laterilaterial which tables as about the number of violated constraints.

 $H(\sigma) = \sum_{ij} \frac{M}{2} \chi^{\frac{i(j-j)}{2} \prod_{i \neq j} \sigma_{i,j}}$ 



Hittle connectivity is more restistic than fully connected and same argument applies for vector spins over fairg spins. Pinitely commoded connected spins was investigated upon. Vactor spins five on a sphere  $|a_{2}, b_{2-1}|$  with random matrix interactions.

all where  $V_{ij}$  are unitary matrices representing rotations in  $\mathbb{R}^d$  which are drawn randomly and independently from section matrix ensemble P(V) and P(V) = P(V) (and  $V(v_i)$  is the omitis potential.

 $Z_i^{(I)}(z_i) = \int_{\mathbb{R}^n} \int_{\mathbb{R}^n} \prod_{k \in \mathbb{N}_i} dz_k |exp(i) \int \sum_{k \in \mathbb{N}_i} z_k \Gamma_{ik} z_k$ 

 $W[P] = \sum_{i=0}^{\infty} e^{i \frac{i}{2} t^i} f[\prod_{i=1}^{n} e^{i t_i} W[W[P])] W[\Phi(t_i)]$ 

 $\times \delta_{|f|} |P(\sigma) - \frac{e^{\frac{2(\gamma+1)}{3}} \prod_{i \neq j \text{ deg}} \frac{1}{1 + i f \text{ deg}^{(1+i)} + 0.0}}{\int d\sigma e^{-2(\gamma+1)} \prod_{i \neq j} \frac{1}{1 + i f \text{ deg}^{(2+i)} + 0.00}},$ Order parameter is a functional and thereo functional re-ment separation is required to find phose transitions. Pop-ulation dynamics in this case requires lineating functional which is numerically challenging to perform. Also, numer-cal simulations requires to generate suitable random modi-cal simulations requires to generate suitable random modi-

Fig. 4: July vis phin/intensity

 $H(\{\sigma\}) = \sum_{i=1}^{M} \frac{(1 - \sum_{i \in h_i = i_i \in h_i} J_{i,j}^{(i)})(\prod_{i \in \sigma} \sigma_i J_{i,j}^{(i)})}{2}$ 

where quadruple coupling  $\mathcal{L}_{gal}^{(s)}$  is given warne as in the first

[2] C. Conti and L. Louzzi, Phys. Rev. B 83, 134204(2011); [3] M. Meuzard and G. Parisi, Bur. Phys. J. B 25, 217-233 (2001);

[4] AGG Goden et al., J. Phys. A: Math. Gen. 38 (2005) 6289-6317:

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## The road ahead!

## **Applications of RL**

- speckle free imaging
- cryptography
- medical diagnostic
- biomedical imaging
- laser paints

## **Future possibile fields**

- GPU computing
- Photonics
- Experimental laser
- Neuroscience
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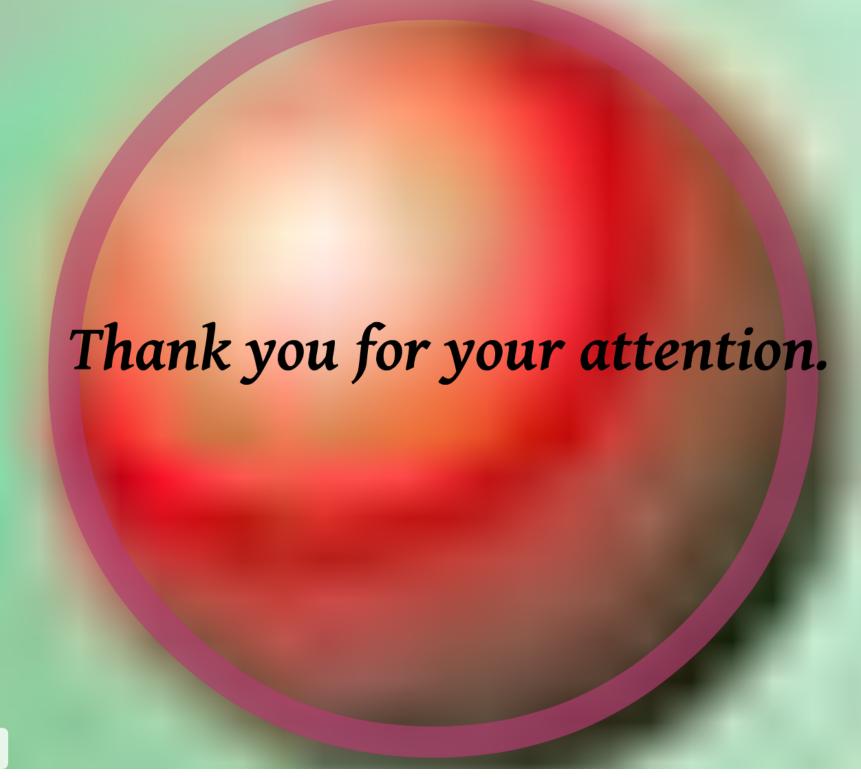
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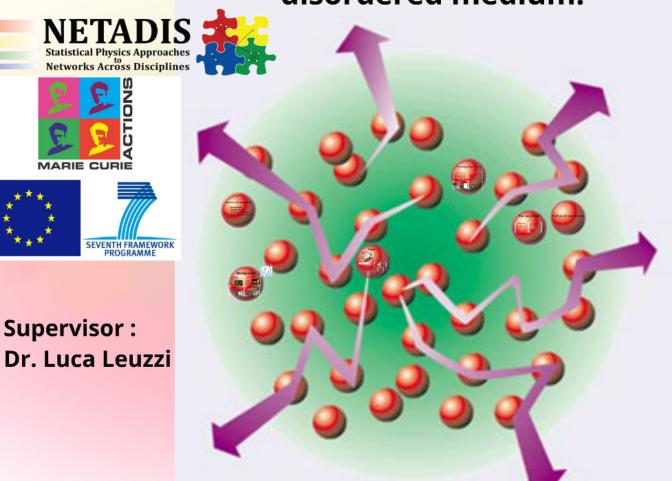
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